

# ECET 257 Power & RF Electronics

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This course is a study of the application of circuit analysis techniques to amplifiers used in power and RF electronics, including bipolar junction transistors, field effect transistors, thyristors, RF amplifiers, phase lock loops, switching power supplies, and appropriate applications. Computer aided analysis of circuits is used.

[Http://www.tech.purdue.edu/eet/courses/eet257/](http://www.tech.purdue.edu/eet/courses/eet257/)

# What will you be able to do?

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## ◆ RF Amplifiers

- $f \leq 100$  MHz

## ◆ Power Electronic Switches

- $I_{\text{on}} = 6 \text{ A}_p$        $V_{\text{off}} = \pm 56 \text{ V}$      $t_{\text{on or off}} < 30\text{ns}$
- Buck power supply       $I_{\text{dc}} = 1 \text{ A}$      $\pm 0.1 \text{ V}_{\text{pp}}$
- Boost power supply     $5 \text{ V}_{\text{dc}}$  to  $15 \text{ V}_{\text{dc}}$     *not* transformer

## ◆ Switching & Linear Amplifier

- $v_{\text{load}} \geq 40 \text{ V}_p$ ,  $8 \Omega$ ,  $100 \Omega$ , protected, 1 % THD
- Sound – room – loudspeaker – amplifier

# What will this *cost*?

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- ◆ How much more work was
  - ECET 207 than EET 107?
  - $\times 1.5$
  
- ◆ ECET 257 requires  $\times 1.25$  more work than ECET 207

# Study !!

There is no substitute  
for *effective* work.

Purdue University

## How to Study for ECET 257

~ 2 hours, five nights per week

Lectures on Monday, Wednesday, and Friday

Lab on Tuesday or Friday

Sim due Monday

Quiz on Friday


- |                  |  |
|------------------|--|
| <b>Monday</b>    | Review all of your class notes<br>Compare them to the web<br><i>Work</i> all calculations from lecture<br>Highlight questions<br>Re-read the text<br><i>Work</i> all of the Practice problems (at the end of every Example in the text)<br>Highlight questions<br>Work the Homework or do the manual calculations for the simulation |
| <b>Tuesday</b>   | Find answers to all of your questions, from Monday's lecture and from the text<br>Work the Homework again<br>Read the assignment for Wednesday<br><i>Work</i> the Examples<br>Highlight questions<br>Rough out the lab report  |
| <b>Wednesday</b> | Review all of your class notes<br>Compare them to the web<br><i>Work</i> all calculations<br>Highlight questions<br>Re-read the text<br><i>Work</i> all of the Practice problems (at the end of every Example in the text)<br>Highlight questions<br>Work the Homework<br>Complete the lab report                                    |
| <b>Thursday</b>  | Find answers to all of your questions, from Wednesday's lecture and from the text<br>Work the Homework <i>again</i><br>Read the assignment for Monday<br><i>Work</i> the Examples<br>Highlight questions<br>Work the Homework <i>again</i><br>Begin the Simulation due Monday<br>Review for Quiz                                     |
| <b>Sunday</b>    | Finish the Simulation<br><i>Catch up</i>   |

**ECET 257**










**Consumer Power Electronics**

**Fall 2010**

**Course Information**

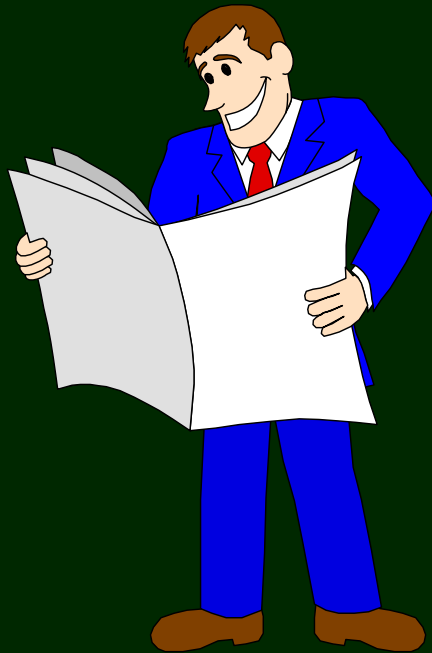
Clicking on this  icon will allow you to attend the class virtually; M-W-F 2:30-3:20.

Clicking on the same icon on a specific date, below, allows you to watch the recorded version of the class. If the class has not yet happened for the Fall 2010 semester, then you will be served that class from the Spring 2010 semester.

	Monday	Wednesday	Friday	Lab
Aug Week 1	23 <a href="#">Intro Pwr</a>  read: text Chapter 3 assess: none	25 <a href="#">Power Calculations</a> read: text chapter 3 assess: <a href="#">01-PowerCalc1</a>	27 <a href="#">Thyristors</a>  read: text p385-396 assess: <a href="#">02-Power Calc2</a>	<a href="#">Power Parameter Calculations</a>
Aug/Sep 2	30 <a href="#">DigitalCntrThy</a>  read: text 403-409 assess: <a href="#">04-Thyristors</a>	1 <a href="#">Phase Angle Firing</a>  read: text p417-430 Only <i>audio</i> assess: <a href="#">Thyristors Sim</a>	3 <a href="#">Snubbing</a> read: text p396-403 assess: <a href="#">05-PhaseAngleFired</a>	<a href="#">Triac - Logic Control</a>  <a href="#">Screen Captures</a>
3	6 No Class  <b>Labor Day</b>	8 <a href="#">High Freq</a>  read: none assess: <a href="#">Phase Angle Fire Sim</a>	10 <a href="#">Problem Session</a>  read: none <i>no audio</i> assess: <a href="#">03-HighFreqEffects</a>	<a href="#">Triac - Analog Control</a>
4	13  <b>Exam 1</b>	15 <a href="#">Low-Side BJT</a>  read: text p269-277 <i>no audio</i> assess: none	17 <a href="#">LS MOS Analy</a>  read: text p278-286 assess: <a href="#">06-LS BJT AnalyHS</a>	High Frequency Considerations
5	20 <a href="#">Highside Analy</a>  read: text p295-303 assess: <a href="#">07-LS MOS Analy</a>	22 <a href="#">Heat Sinks</a>  read: text p176-181 assess: <a href="#">HS Switch Sim</a>	12 <a href="#">LS Switch Des</a>  read: text 269-304 assess: <a href="#">09-Heat Sinks</a>	Switch Analysis  <a href="#">Example Layout Photo</a>
Sep/Oct 6	27 <a href="#">HS Switch Design</a>  read: text p295-303 assess: <a href="#">Low-side Design Sim</a>	29 <a href="#">MOS Drivers</a>  read: text 304-308 assess: <a href="#">10-HS Design</a>	1 <a href="#">H-Bridges</a>  read: text 309-314 assess: <a href="#">11-MOS Drivers</a>	Switch Design
Oct 7	4  <b>Exam 2</b>	6 <a href="#">Buck Principles</a>  read: text p326-337 <i>no audio</i> assess: none	8 <a href="#">LM3578 Buck</a>  read: National Semi data assess: <a href="#">12a-Buck</a>	MOS Driver  <a href="#">Layout photo</a>
8	11 No Class  <b>October Break</b>	13 <a href="#">Problem Session</a> read: none assess: <a href="#">Buck Sim</a>	15 <a href="#">Boost Principles</a>  read: text p344-352 assess: <a href="#">12b-BuckIC</a>	Buck Regulator

# Syllabus

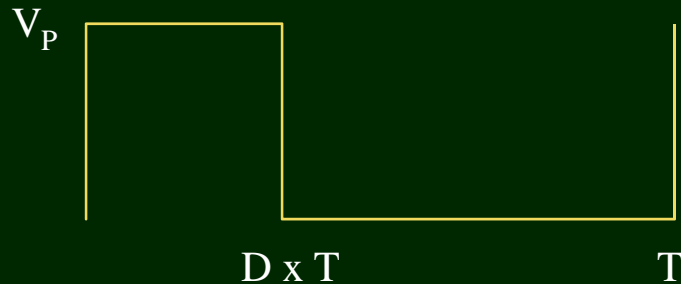
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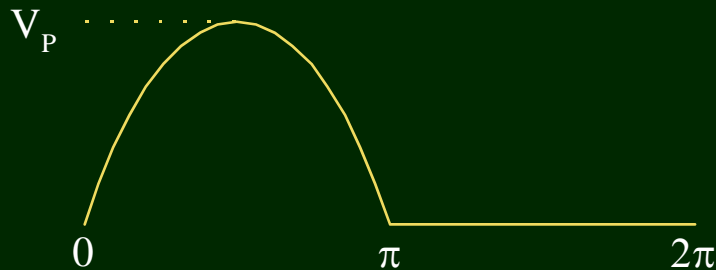
- ◆ It is a contract.
  - Read it! Use it!
- ◆ 8. Professional conduct
- ◆ 9. Cheating
- ◆ Simulation\*, HW, Quizzes,
- ◆ Labs\*
- ◆ Grading Policy
- ◆ Standards: HW, Lab Reports

\* *Must* pass Simulation & Lab to pass the course.

# Average, RMS, and Power



$$V_{\text{ave}} = \frac{1}{T} \int_0^T v(t) dt$$



$$V_{\text{RMS}} = \sqrt{\frac{1}{T} \left( \int v^2(t) dt \right)}$$

$$P = \frac{1}{2\pi} \left[ \int_0^{\pi} (V_P \sin \theta)(I_P \sin \theta) d\theta + \int_{\pi}^{2\pi} 0 d\theta \right]$$

# Overview

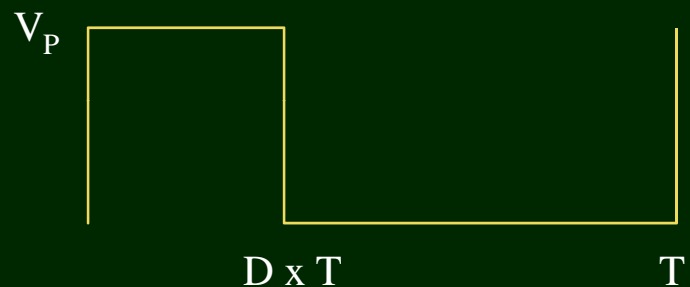
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- ◆ Average
  - definition      integrals
  - pulse    half sine                  table
  
- ◆ Root Mean Squared
  - definition      integrals
  - table
  
- ◆ Power
  - definition
  - pulse    half sine                  table

# Average Value:

# definition

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# Average Value: definition

---

- ◆ average height
- ◆ area under the curve / length



# Average Value:

# definition

◆ average height

◆ area under the curve / length



$$V_{ave} = \frac{1}{T} \int_0^T v(t) dt$$

# Average Value: definition

◆ average height

◆ area under the curve / length



$$V_{ave} = \frac{1}{T} \int_0^T v(t) dt$$

# Average Value:

# pulse

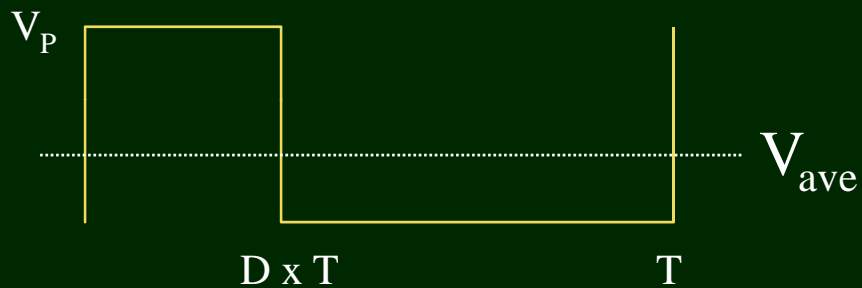
$$V_{\text{ave}} = \frac{1}{T} \int_0^T v(t) dt$$



$$v(t) = \begin{cases} V_P & 0 < t < DT \\ 0 & DT < t < T \end{cases} \quad 0 < D < 1$$

# Average Value:

# pulse



$$v(t) = \begin{cases} V_P & 0 < t < DT \\ 0 & DT < t < T \end{cases} \quad 0 < D < 1$$

$$\begin{aligned} V_{ave} &= \frac{1}{T} \int_0^T v(t) dt \\ &= \frac{1}{T} \left( \int_0^{DT} V_P dt + \int_{DT}^T 0 dt \right) \end{aligned}$$

# Average Value:

# pulse



$$v(t) = \begin{cases} V_P & 0 < t < DT \\ 0 & DT < t < T \end{cases} \quad 0 < D < 1$$

$$\begin{aligned} V_{ave} &= \frac{1}{T} \int_0^T v(t) dt \\ &= \frac{1}{T} \left( \int_0^{DT} V_P dt + \int_{DT}^T 0 dt \right) \\ &= \frac{V_P}{T} \int_0^{DT} dt \end{aligned}$$

## Average Value:

## pulse



$$v(t) = \begin{cases} V_P & 0 < t < DT \\ 0 & DT < t < T \end{cases} \quad 0 < D < 1$$

$$\begin{aligned} V_{\text{ave}} &= \frac{1}{T} \int_0^T v(t) dt \\ &= \frac{1}{T} \left( \int_0^{DT} V_P dt + \int_{DT}^T 0 dt \right) \\ &= \frac{V_P}{T} \int_0^{DT} dt \\ &= \frac{V_P}{T} \left( t \Big|_0^{DT} \right) \end{aligned}$$

## Average Value:

## pulse



$$v(t) = \begin{cases} V_P & 0 < t < DT \\ 0 & DT < t < T \end{cases} \quad 0 < D < 1$$

$$\begin{aligned} V_{\text{ave}} &= \frac{1}{T} \int_0^T v(t) dt \\ &= \frac{1}{T} \left( \int_0^{DT} V_P dt + \int_{DT}^T 0 dt \right) \\ &= \frac{V_P}{T} \int_0^{DT} dt \\ &= \frac{V_P}{T} \left( t \Big|_0^{DT} \right) \\ &= \frac{V_P}{T} (DT - 0) \end{aligned}$$

## Average Value:

## pulse



$$v(t) = \begin{cases} V_P & 0 < t < DT \\ 0 & DT < t < T \end{cases} \quad 0 < D < 1$$

$$\begin{aligned} V_{\text{ave}} &= \frac{1}{T} \int_0^T v(t) dt \\ &= \frac{1}{T} \left( \int_0^{DT} V_P dt + \int_{DT}^T 0 dt \right) \\ &= \frac{V_P}{T} \int_0^{DT} dt \\ &= \frac{V_P}{T} \left( t \Big|_0^{DT} \right) \\ &= \frac{V_P}{T} (DT - 0) \end{aligned}$$

$$V_{\text{ave}} = DV_P$$

# Average Value:

# pulse



$$v(t) = \begin{cases} V_P & 0 < t < DT \\ 0 & DT < t < T \end{cases} \quad 0 < D < 1$$

$$V_{ave} = DV_P$$

$$T = 5 \text{ ms}$$

$$t_{\text{pulse width}} = 2 \text{ ms}$$

$$D = ?$$

$$V_p = 10 \text{ V}_p$$

$$V_{ave} = ?$$

# Average Value:

# pulse



$$v(t) = \begin{cases} V_P & 0 < t < DT \\ 0 & DT < t < T \end{cases} \quad 0 < D < 1$$

$$V_{ave} = DV_P$$

$$T = 5 \text{ ms}$$

$$t_{\text{pulse width}} = 2 \text{ ms}$$

$$D = 0.4$$

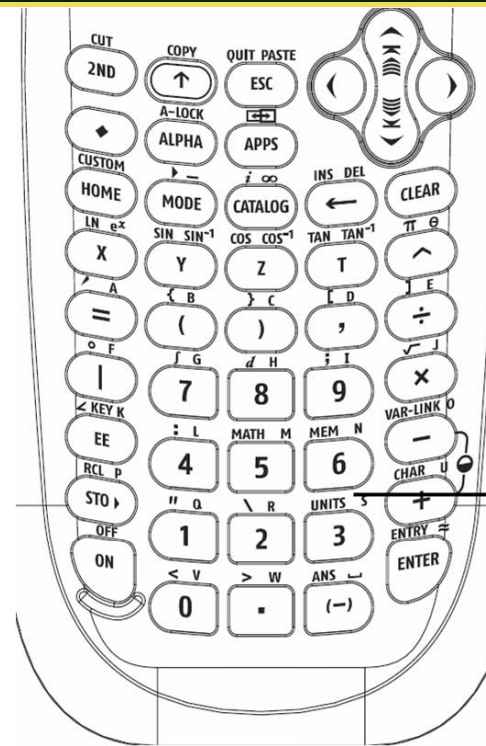
$$V_p = 10 \text{ V}_p$$

$$V_{ave} = 4 \text{ V}_p$$

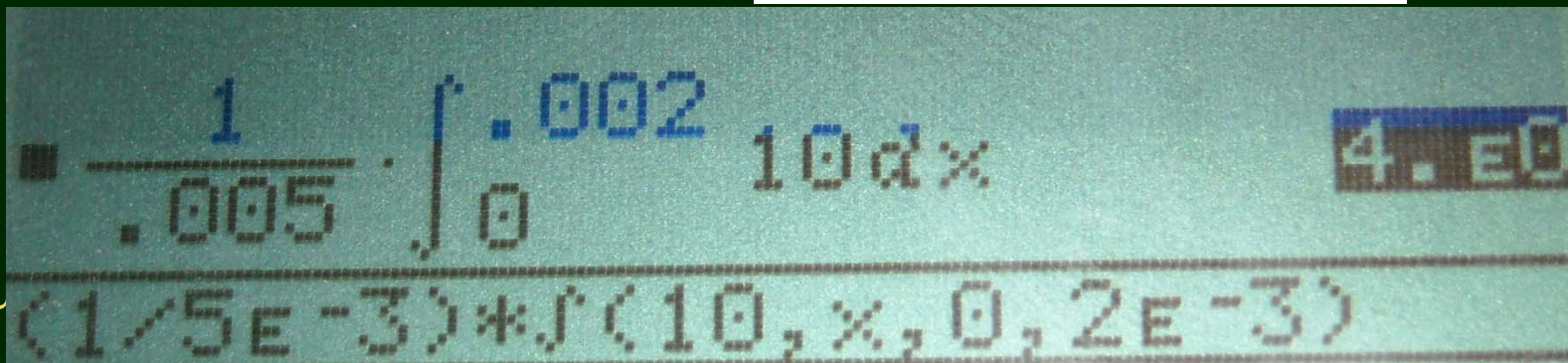
# Average Value:

# pulse

$$\begin{aligned}
 V_{ave} &= \frac{1}{T} \int_0^T v(t) dt \\
 &= \frac{1}{T} \left( \int_0^{DT} V_P dt + \int_{DT}^T 0 dt \right) \\
 &= \frac{1}{5\text{ms}} \left( \int_0^{2\text{ms}} 10V_P dt \right)
 \end{aligned}$$



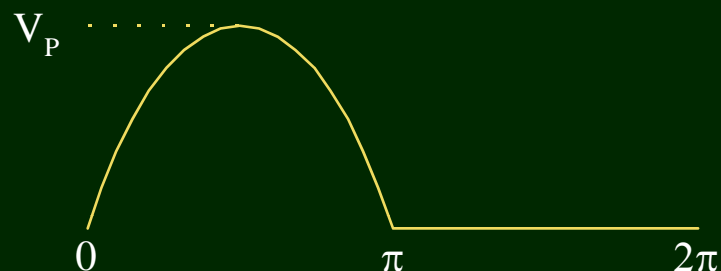
[http://education.ti.com/downloads/guidebooks/graphing/89ti/TI89TitaniumGuidebook\\_Part2\\_EN.pdf](http://education.ti.com/downloads/guidebooks/graphing/89ti/TI89TitaniumGuidebook_Part2_EN.pdf)



# Average Value:

# half sine

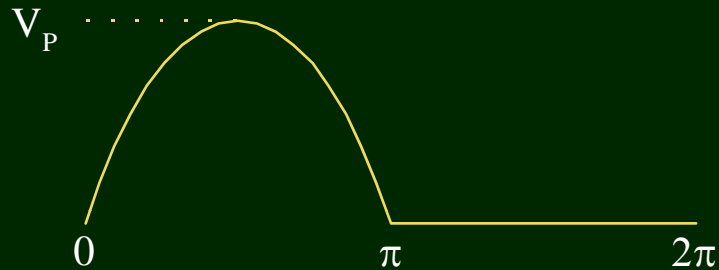
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$$v(\theta) = \begin{cases} V_P \sin \theta & 0 < \theta < \pi \\ 0 & \pi < \theta < 2\pi \end{cases}$$

# Average Value:

# half sine

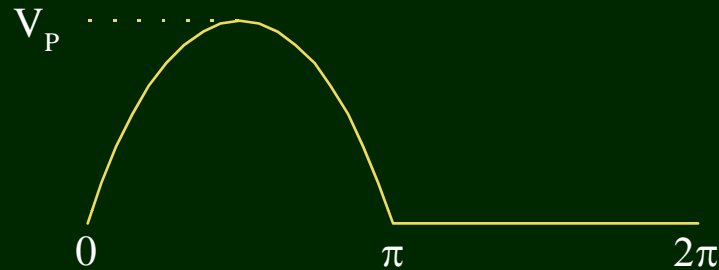


$$v(\theta) = \begin{cases} V_P \sin \theta & 0 < \theta < \pi \\ 0 & \pi < \theta < 2\pi \end{cases}$$

$$V_{\text{ave}} = \frac{1}{T} \int_0^T v(t) dt$$

# Average Value:

# half sine

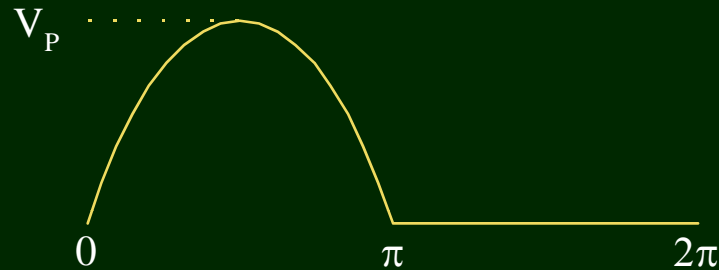


$$v(\theta) = \begin{cases} V_P \sin \theta & 0 < \theta < \pi \\ 0 & \pi < \theta < 2\pi \end{cases}$$

$$\begin{aligned} V_{\text{ave}} &= \frac{1}{T} \int_0^T v(t) dt \\ &= \frac{V_P}{2\pi} \left( \int_0^\pi \sin \theta d\theta + \int_\pi^{2\pi} 0 d\theta \right) \end{aligned}$$

# Average Value:

# half sine

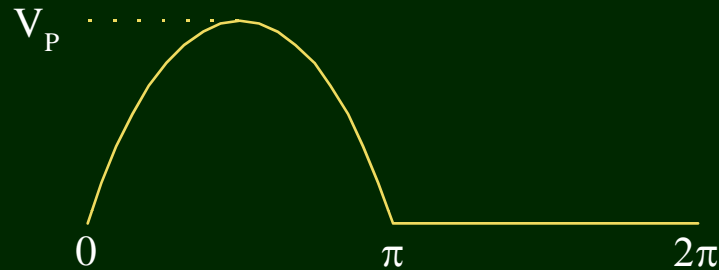


$$v(\theta) = \begin{cases} V_P \sin \theta & 0 < \theta < \pi \\ 0 & \pi < \theta < 2\pi \end{cases}$$

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# Average Value:

# half sine

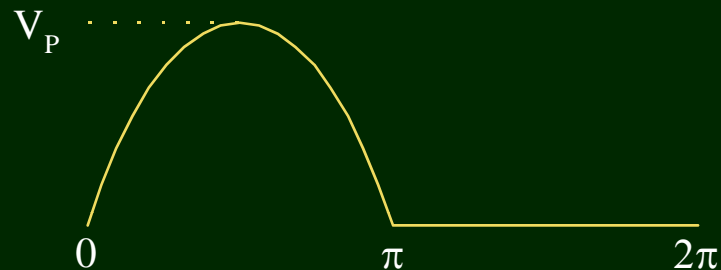


$$v(\theta) = \begin{cases} V_P \sin \theta & 0 < \theta < \pi \\ 0 & \pi < \theta < 2\pi \end{cases}$$

$$\begin{aligned} V_{\text{ave}} &= \frac{1}{T} \int_0^T v(t) dt \\ &= \frac{V_P}{2\pi} \left( \int_0^\pi \sin \theta d\theta + \int_\pi^{2\pi} 0 d\theta \right) \\ &= \frac{V_P}{2\pi} \int_0^\pi \sin \theta d\theta \\ &= \frac{V_P}{2\pi} \left( -\cos \theta \Big|_0^\pi \right) \end{aligned}$$

# Average Value:

# half sine

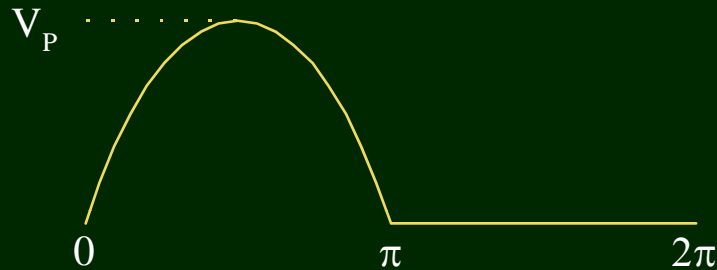


$$v(\theta) = \begin{cases} V_P \sin \theta & 0 < \theta < \pi \\ 0 & \pi < \theta < 2\pi \end{cases}$$

$$\begin{aligned} V_{\text{ave}} &= \frac{1}{T} \int_0^T v(t) dt \\ &= \frac{V_P}{2\pi} \left( \int_0^\pi \sin \theta d\theta + \int_\pi^{2\pi} 0 d\theta \right) \\ &= \frac{V_P}{2\pi} \int_0^\pi \sin \theta d\theta \\ &= \frac{V_P}{2\pi} \left( -\cos \theta \Big|_0^\pi \right) \\ &= \frac{V_P}{2\pi} (-\cos \pi + \cos 0) \end{aligned}$$

## Average Value:

## half sine

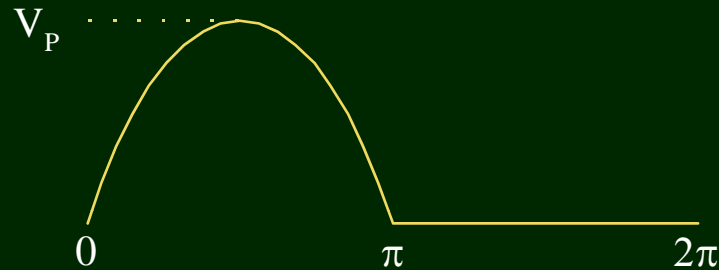


$$v(\theta) = \begin{cases} V_P \sin \theta & 0 < \theta < \pi \\ 0 & \pi < \theta < 2\pi \end{cases}$$

$$\begin{aligned} V_{\text{ave}} &= \frac{1}{T} \int_0^T v(t) dt \\ &= \frac{V_P}{2\pi} \left( \int_0^\pi \sin \theta d\theta + \int_\pi^{2\pi} 0 d\theta \right) \\ &= \frac{V_P}{2\pi} \int_0^\pi \sin \theta d\theta \\ &= \frac{V_P}{2\pi} \left( -\cos \theta \Big|_0^\pi \right) \\ &= \frac{V_P}{2\pi} (-\cos \pi + \cos 0) \\ &= \frac{V_P}{2\pi} (-(-1) + 1) \end{aligned}$$

# Average Value:

# half sine

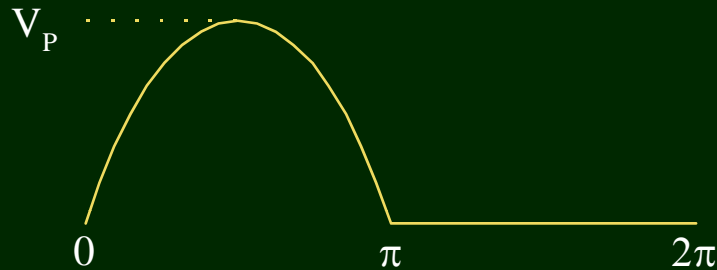


$$v(\theta) = \begin{cases} V_P \sin \theta & 0 < \theta < \pi \\ 0 & \pi < \theta < 2\pi \end{cases}$$

$$\begin{aligned} V_{\text{ave}} &= \frac{1}{T} \int_0^T v(t) dt \\ &= \frac{V_P}{2\pi} \left( \int_0^\pi \sin \theta d\theta + \int_\pi^{2\pi} 0 d\theta \right) \\ &= \frac{V_P}{2\pi} \int_0^\pi \sin \theta d\theta \\ &= \frac{V_P}{2\pi} \left( -\cos \theta \Big|_0^\pi \right) \\ &= \frac{V_P}{2\pi} (-\cos \pi + \cos 0) \\ &= \frac{V_P}{2\pi} (-(-1) + 1) \\ &= \frac{2V_P}{2\pi} \end{aligned}$$

# Average Value:

# half sine



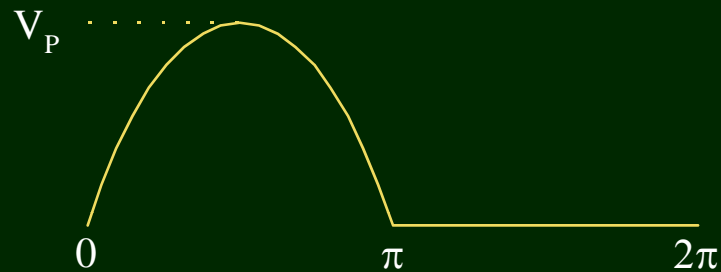
$$v(\theta) = \begin{cases} V_P \sin \theta & 0 < \theta < \pi \\ 0 & \pi < \theta < 2\pi \end{cases}$$

$$\begin{aligned} V_{\text{ave}} &= \frac{1}{T} \int_0^T v(t) dt \\ &= \frac{V_P}{2\pi} \left( \int_0^\pi \sin \theta d\theta + \int_\pi^{2\pi} 0 d\theta \right) \\ &= \frac{V_P}{2\pi} \int_0^\pi \sin \theta d\theta \\ &= \frac{V_P}{2\pi} \left( -\cos \theta \Big|_0^\pi \right) \\ &= \frac{V_P}{2\pi} (-\cos \pi + \cos 0) \\ &= \frac{V_P}{2\pi} (-(-1) + 1) \\ &= \frac{2V_P}{2\pi} \end{aligned}$$

$$V_{\text{ave}} = \frac{V_P}{\pi}$$

# Average Value:

# half sine



$$v(\theta) = \begin{cases} V_P \sin \theta & 0 < \theta < \pi \\ 0 & \pi < \theta < 2\pi \end{cases}$$

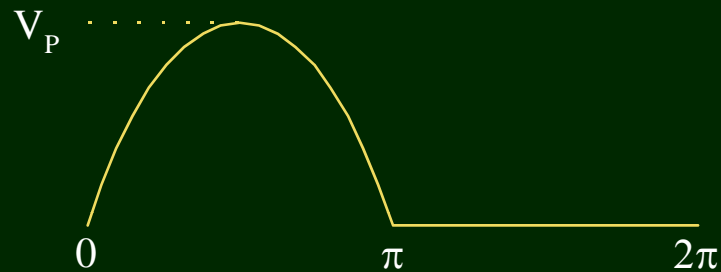
$$V_{ave} = \frac{V_P}{\pi}$$

$$V_p = 170 V_p$$

$$V_{ave} = ?$$

# Average Value:

# half sine



$$v(\theta) = \begin{cases} V_P \sin \theta & 0 < \theta < \pi \\ 0 & \pi < \theta < 2\pi \end{cases}$$

$$V_{ave} = \frac{V_P}{\pi}$$

$$V_p = 170 V_p$$

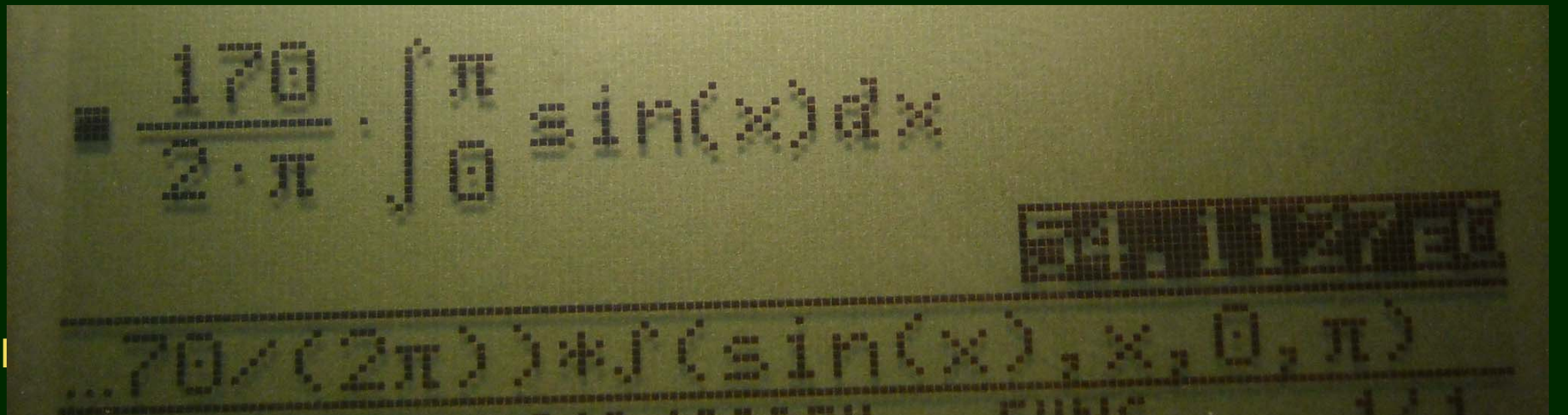
$$V_{ave} = 54 V_{dc}$$

# Average Value:

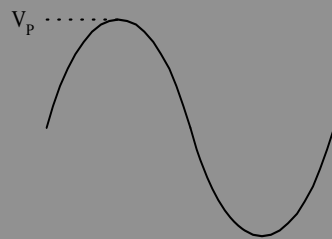
# half sine

Set calculator to *radians*.

$$\begin{aligned}
 V_{ave} &= \frac{1}{T} \int_0^T v(t) dt \\
 &= \frac{V_P}{2\pi} \left( \int_0^\pi \sin \theta d\theta + \int_\pi^{2\pi} 0 d\theta \right) \\
 &= \frac{V_P}{2\pi} \int_0^\pi \sin \theta d\theta \\
 &= (170 / (2\pi)) * \int (\sin(X), X, 0, \pi)
 \end{aligned}$$



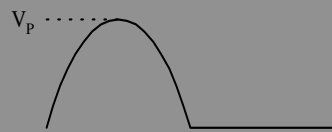
A  
v  
e  
r  
a  
g  
e  
  
V  
a  
l  
u  
e



$$v(\theta) = V_p \sin \theta$$

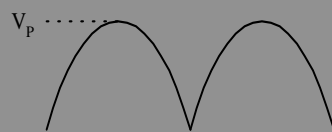
average

0



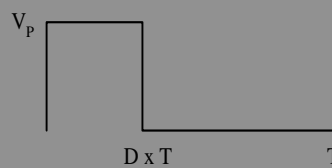
$$v(\theta) = \begin{cases} V_p \sin \theta & 0 < \theta < \pi \\ 0 & \pi < \theta < 2\pi \end{cases}$$

$\frac{V_p}{\pi}$



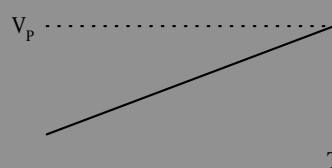
$$v(\theta) = \begin{cases} V_p \sin \theta & 0 < \theta < \pi \\ -V_p \sin \theta & \pi < \theta < 2\pi \end{cases}$$

$\frac{2V_p}{\pi}$



$$v(t) = \begin{cases} V_p & 0 < t < DT \\ 0 & DT < t < T \end{cases} \quad 0 < D < 1$$

$DV_p$



$$v(t) = \frac{V_p}{T} t$$

$\frac{V_p}{2}$

# Overview

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- ◆ Average

- definition integrals
- pulse half sine table



## Root Mean Squared

- definition integrals
- table

- ◆ Power

- definition
- pulse half sine table

# Root Mean Squared: definition

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- ◆ All signals of equal  $V_{\text{RMS}}$   $\Rightarrow$  *same power*
- ◆  $p \Rightarrow v^2$  or  $i^2$
- ◆  $P_{\text{ave}}$  not  $p(t)$   $\Rightarrow$  *integral of square*
- ◆ *square root* to get back to volts or amps
- ◆ root mean squared

# Root Mean Squared:

37  
definition

$$V_{\text{RMS}} = \sqrt{\frac{1}{T} \left( \int v^2(t) dt \right)}$$

# Root Mean Squared:

# definition

$$V_{\text{RMS}} = \sqrt{\frac{1}{T} \left( \int v^2(t) dt \right)}$$

root

# Root Mean Squared:

# definition

$$V_{\text{RMS}} = \sqrt{\frac{1}{T} \left( \int v^2(t) dt \right)}$$

root

mean

# Root Mean Squared:

# definition

$$V_{\text{RMS}} = \sqrt{\frac{1}{T} \left( \int v^2(t) dt \right)}$$

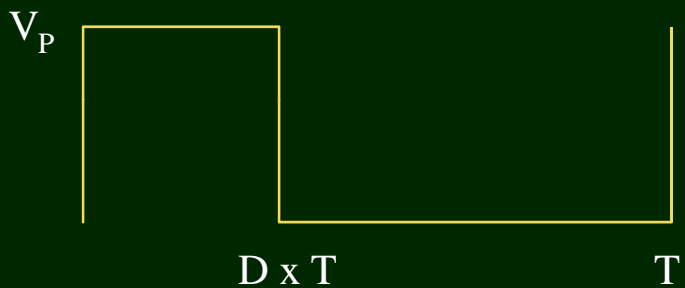
root

mean

squared

# Root Mean Squared:

# pulse



$$v(t) = \begin{cases} V_P & 0 < t < DT \\ 0 & DT < t < T \end{cases} \quad 0 < D < 1$$

$$V_{\text{RMS}} = \sqrt{\frac{1}{T} \left( \int v^2(t) dt \right)}$$

$$V_{\text{RMS}} = \sqrt{\frac{1}{T} \left( \int_0^{DT} V_P^2 dt + \int_{DT}^T 0 dt \right)}$$

$$= \sqrt{\frac{V_P^2}{T} \left( \int_0^{DT} dt \right)}$$

$$= \frac{V_P}{\sqrt{T}} \sqrt{(t) \Big|_0^{DT}}$$

$$= \frac{V_P}{\sqrt{T}} \sqrt{(DT) - (0)}$$

$$= \frac{V_P}{\sqrt{T}} \sqrt{DT}$$

$$V_{\text{RMS}} = \sqrt{D} \times V_P$$

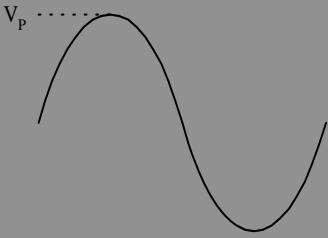
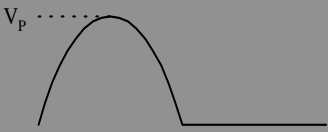
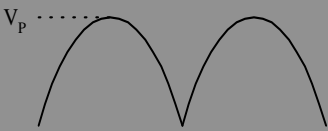
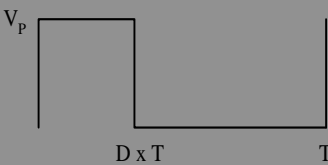
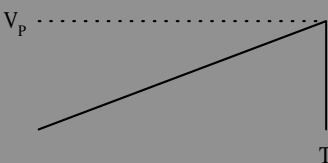
	<u>function</u>	<u>average</u>	<u>RMS</u>
	$v(\theta) = V_p \sin \theta$	0	$\frac{V_p}{\sqrt{2}}$
	$v(\theta) = \begin{cases} V_p \sin \theta & 0 < \theta < \pi \\ 0 & \pi < \theta < 2\pi \end{cases}$	$\frac{V_p}{\pi}$	$\frac{V_p}{2}$
	$v(\theta) = \begin{cases} V_p \sin \theta & 0 < \theta < \pi \\ -V_p \sin \theta & \pi < \theta < 2\pi \end{cases}$	$\frac{2V_p}{\pi}$	$\frac{V_p}{\sqrt{2}}$
	$v(t) = \begin{cases} V_p & 0 < t < DT \\ 0 & DT < t < T \end{cases} \quad 0 < D < 1$	$DV_p$	$\sqrt{D} \times V_p$
	$v(t) = \frac{V_p}{T} t$	$\frac{V_p}{2}$	$\frac{V_p}{\sqrt{3}}$

Table 3-1

p137

# Overview

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- ◆ Average

- definition      integrals
- pulse    half sine      table

- ◆ Root Mean Squared

- definition      integrals
- table



- ◆ Power

- definition
- pulse    half sine      table

# Power:

# definition

---

 $p(t)$ 

instantaneous power

 $v(t) \times i(t)$  $P_{\text{ave}}$ 

average  $p(t)$

# Power:

# definition

---

$p(t)$

instantaneous power

$$v(t) \times i(t)$$

$P_{\text{ave}}$

average  $p(t)$

$$= \frac{1}{T} \int_0^T v(t) \times i(t) dt$$

# Power:

# definition

---

$p(t)$

instantaneous power

$$v(t) \times i(t)$$

$P_{\text{ave}}$

average  $p(t)$

$$= \frac{1}{T} \int_0^T v(t) \times i(t) dt$$

$$\neq V_{RMS} I_{RMS}$$

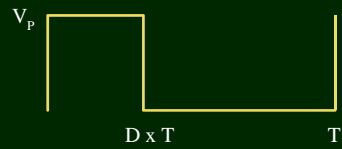
# Power: pulse into a resistor

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$$v(t) = \begin{cases} V_p & 0 < t < DT \\ 0 & DT < t < T \end{cases} \quad 0 < D < 1$$

# Power: pulse into a resistor

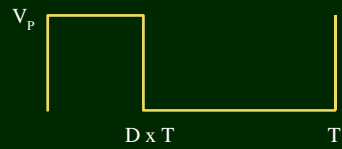


$$v(t) = \begin{cases} V_p & 0 < t < DT \\ 0 & DT < t < T \end{cases} \quad 0 < D < 1$$



$$i(t) = \begin{cases} I_p & 0 < t < DT \\ 0 & DT < t < T \end{cases} \quad 0 < D < 1$$

# Power: pulse into a resistor



$$v(t) = \begin{cases} V_p & 0 < t < DT \\ 0 & DT < t < T \end{cases} \quad 0 < D < 1$$



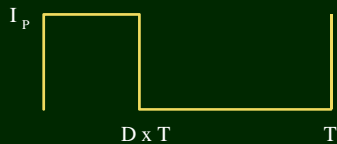
$$i(t) = \begin{cases} I_p & 0 < t < DT \\ 0 & DT < t < T \end{cases} \quad 0 < D < 1$$

$$P = p_{ave} = ave[v(t) \times i(t)]$$

# Power: pulse into a resistor



$$v(t) = \begin{cases} V_P & 0 < t < DT \\ 0 & DT < t < T \end{cases} \quad 0 < D < 1$$

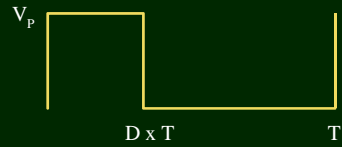


$$i(t) = \begin{cases} I_P & 0 < t < DT \\ 0 & DT < t < T \end{cases} \quad 0 < D < 1$$

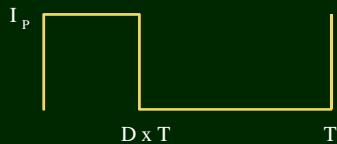
$$P = p_{ave} = ave[v(t) \times i(t)]$$

$$P = \frac{1}{T} \left[ \int_0^{DT} V_P I_P dt + \int_{DT}^T 0 dt \right]$$

# Power: pulse into a resistor



$$v(t) = \begin{cases} V_P & 0 < t < DT \\ 0 & DT < t < T \end{cases} \quad 0 < D < 1$$



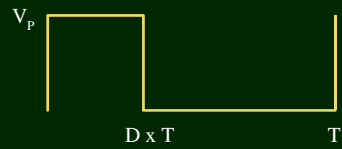
$$i(t) = \begin{cases} I_P & 0 < t < DT \\ 0 & DT < t < T \end{cases} \quad 0 < D < 1$$

$$P = p_{ave} = ave[v(t) \times i(t)]$$

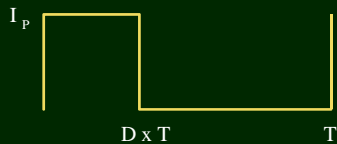
$$P = \frac{1}{T} \left[ \int_0^{DT} V_P I_P dt + \int_{DT}^T 0 dt \right]$$

$$= \frac{1}{T} \int_0^{DT} V_P I_P dt$$

# Power: pulse into a resistor



$$v(t) = \begin{cases} V_P & 0 < t < DT \\ 0 & DT < t < T \end{cases} \quad 0 < D < 1$$



$$i(t) = \begin{cases} I_P & 0 < t < DT \\ 0 & DT < t < T \end{cases} \quad 0 < D < 1$$

$$P = p_{ave} = ave[v(t) \times i(t)]$$

$$P = \frac{1}{T} \left[ \int_0^{DT} V_P I_P dt + \int_{DT}^T 0 dt \right]$$

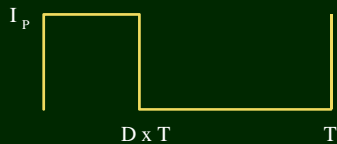
$$= \frac{1}{T} \int_0^{DT} V_P I_P dt$$

$$= \frac{V_P I_P}{T} \int_0^{DT} dt$$

# Power: pulse into a resistor



$$v(t) = \begin{cases} V_P & 0 < t < DT \\ 0 & DT < t < T \end{cases} \quad 0 < D < 1$$



$$i(t) = \begin{cases} I_P & 0 < t < DT \\ 0 & DT < t < T \end{cases} \quad 0 < D < 1$$

$$P = p_{ave} = ave[v(t) \times i(t)]$$

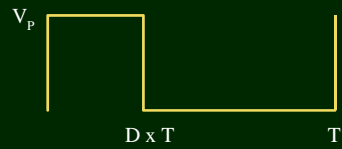
$$P = \frac{1}{T} \left[ \int_0^{DT} V_P I_P dt + \int_{DT}^T 0 dt \right]$$

$$= \frac{1}{T} \int_0^{DT} V_P I_P dt$$

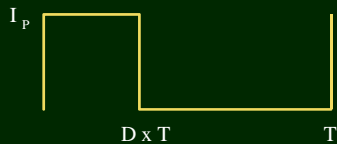
$$= \frac{V_P I_P}{T} \int_0^{DT} dt$$

$$= \frac{V_P I_P}{T} \left[ t \Big|_0^{DT} \right]$$

# Power: pulse into a resistor



$$v(t) = \begin{cases} V_P & 0 < t < DT \\ 0 & DT < t < T \end{cases} \quad 0 < D < 1$$



$$i(t) = \begin{cases} I_P & 0 < t < DT \\ 0 & DT < t < T \end{cases} \quad 0 < D < 1$$

$$P = p_{ave} = ave[v(t) \times i(t)]$$

$$P = \frac{1}{T} \left[ \int_0^{DT} V_P I_P dt + \int_{DT}^T 0 dt \right]$$

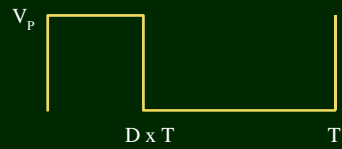
$$= \frac{1}{T} \int_0^{DT} V_P I_P dt$$

$$= \frac{V_P I_P}{T} \int_0^{DT} dt$$

$$= \frac{V_P I_P}{T} \left[ t \Big|_0^{DT} \right]$$

$$= \frac{V_P I_P}{T} [DT - 0]$$

# Power: pulse into a resistor



$$v(t) = \begin{cases} V_P & 0 < t < DT \\ 0 & DT < t < T \end{cases} \quad 0 < D < 1$$



$$i(t) = \begin{cases} I_P & 0 < t < DT \\ 0 & DT < t < T \end{cases} \quad 0 < D < 1$$

$$P = p_{ave} = ave[v(t) \times i(t)]$$

$$P = \frac{1}{T} \left[ \int_0^{DT} V_P I_P dt + \int_{DT}^T 0 dt \right]$$

$$= \frac{1}{T} \int_0^{DT} V_P I_P dt$$

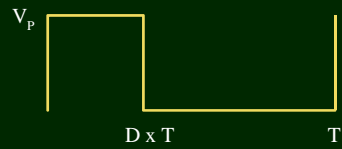
$$= \frac{V_P I_P}{T} \int_0^{DT} dt$$

$$= \frac{V_P I_P}{T} \left[ t \Big|_0^{DT} \right]$$

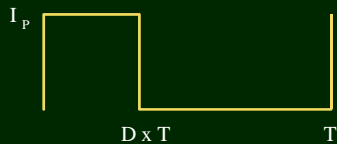
$$= \frac{V_P I_P}{T} [DT - 0]$$

$$P = DV_P I_P$$

# Power: pulse into a resistor



$$v(t) = \begin{cases} V_P & 0 < t < DT \\ 0 & DT < t < T \end{cases} \quad 0 < D < 1$$



$$i(t) = \begin{cases} I_P & 0 < t < DT \\ 0 & DT < t < T \end{cases} \quad 0 < D < 1$$

$$P = p_{ave} = ave[v(t) \times i(t)]$$

$$P = \frac{1}{T} \left[ \int_0^{DT} V_P I_P dt + \int_{DT}^T 0 dt \right]$$

$$P = DV_P I_P$$

$$T = 12 \mu s$$

$$t_{\text{pulse width}} = 8 \mu s$$

$$D = ?$$

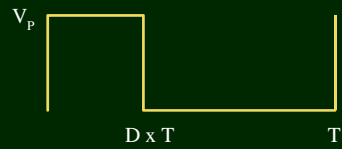
$$V_p = 28 V_p$$

$$R_{\text{load}} = 8 \Omega$$

$$I_p = ?$$

$$P_{ave} = ?$$

# Power: pulse into a resistor



$$v(t) = \begin{cases} V_P & 0 < t < DT \\ 0 & DT < t < T \end{cases} \quad 0 < D < 1$$



$$i(t) = \begin{cases} I_P & 0 < t < DT \\ 0 & DT < t < T \end{cases} \quad 0 < D < 1$$

$$P = p_{ave} = ave[v(t) \times i(t)]$$

$$P = \frac{1}{T} \left[ \int_0^{DT} V_P I_P dt + \int_{DT}^T 0 dt \right]$$

$$P = DV_P I_P$$

$$T = 12 \mu s$$

$$t_{\text{pulse width}} = 8 \mu s$$

$$D = 0.67$$

$$V_p = 28 V_p$$

$$R_{\text{load}} = 8 \Omega$$

$$I_p = 3.5 A_p$$

$$P_{ave} = 65.66 W$$

# Power: pulse into a resistor

$$P = p_{ave} = ave[v(t) \times i(t)]$$

$$P = \frac{1}{T} \left[ \int_0^{DT} V_P I_P dt + \int_{DT}^T 0 dt \right]$$

$$P = \frac{1}{12 \mu s} \left[ \int_0^{8 \mu s} (28 V_P \times 3.5 A_P) dt \right]$$

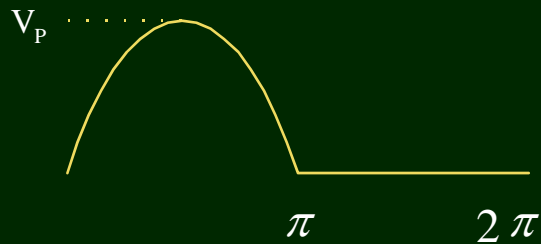
Handwritten calculation on a calculator screen:

$$P = \frac{1}{1.2 \times 10^{-5}} \int_0^{8 \times 10^{-6}} (28 \cdot 3.5) dx$$

$$= 6.666666666666667 \times 10^5 \times (28 \cdot 3.5) \times 0.8 \times 10^{-6}$$

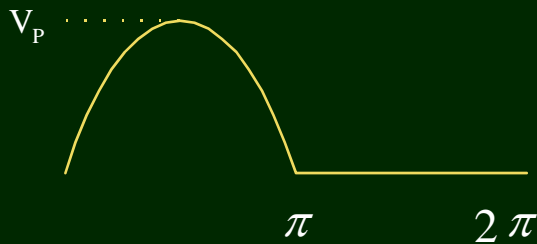
# Power: half sine into a resistor

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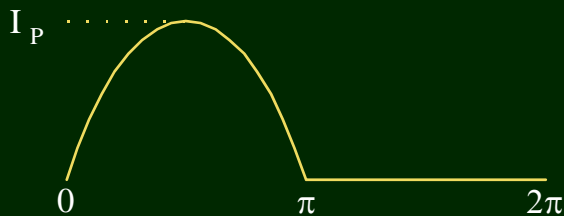


$$v(\theta) = \begin{cases} V_p \sin \theta & 0 < \theta < \pi \\ 0 & \pi < \theta < 2\pi \end{cases}$$

# Power: half sine into a resistor

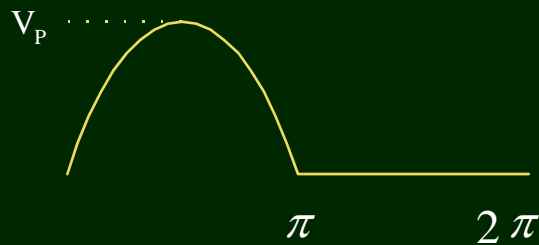


$$v(\theta) = \begin{cases} V_P \sin \theta & 0 < \theta < \pi \\ 0 & \pi < \theta < 2\pi \end{cases}$$

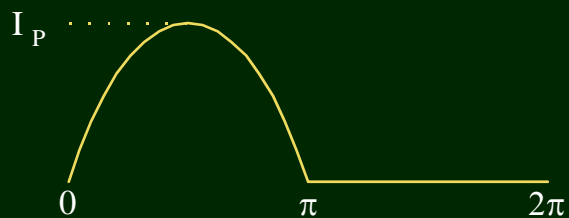


$$i(\theta) = \begin{cases} I_P \sin \theta & 0 < \theta < \pi \\ 0 & \pi < \theta < 2\pi \end{cases}$$

# Power: half sine into a resistor



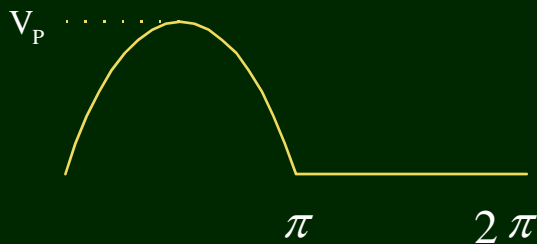
$$v(\theta) = \begin{cases} V_p \sin \theta & 0 < \theta < \pi \\ 0 & \pi < \theta < 2\pi \end{cases}$$



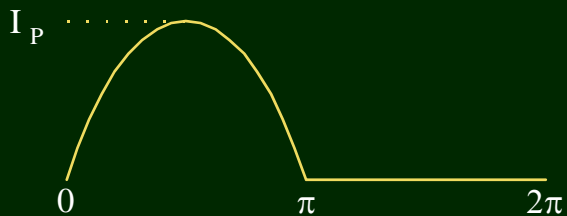
$$i(\theta) = \begin{cases} I_p \sin \theta & 0 < \theta < \pi \\ 0 & \pi < \theta < 2\pi \end{cases}$$

$$P = p_{ave} = ave[v(t) \times i(t)]$$

# Power: half sine into a resistor



$$v(\theta) = \begin{cases} V_p \sin \theta & 0 < \theta < \pi \\ 0 & \pi < \theta < 2\pi \end{cases}$$



$$i(\theta) = \begin{cases} I_p \sin \theta & 0 < \theta < \pi \\ 0 & \pi < \theta < 2\pi \end{cases}$$

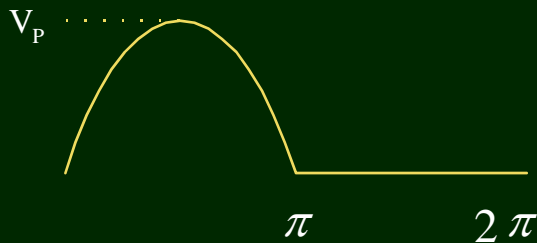
$$P = p_{ave} = ave[v(t) \times i(t)]$$

$$P = \frac{1}{2\pi} \left[ \int_0^\pi (V_p \sin \theta)(I_p \sin \theta) d\theta + \int_\pi^{2\pi} 0 d\theta \right]$$

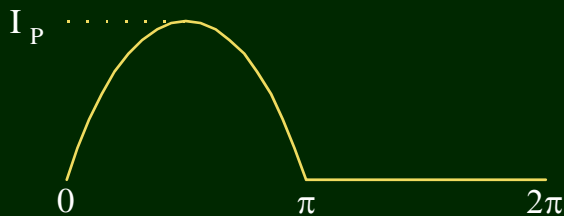
$$V_p = 170 \text{ V}_p \quad R_{load} = 20 \Omega$$

$$I_p = ?$$

# Power: half sine into a resistor



$$v(\theta) = \begin{cases} V_p \sin \theta & 0 < \theta < \pi \\ 0 & \pi < \theta < 2\pi \end{cases}$$



$$i(\theta) = \begin{cases} I_p \sin \theta & 0 < \theta < \pi \\ 0 & \pi < \theta < 2\pi \end{cases}$$

$$P = p_{ave} = ave[v(t) \times i(t)]$$

$$P = \frac{1}{2\pi} \left[ \int_0^\pi (V_p \sin \theta)(I_p \sin \theta) d\theta + \int_\pi^{2\pi} 0 d\theta \right]$$

$$V_p = 170 \text{ V}_p \quad R_{load} = 20 \Omega$$

$$I_p = 8.5 \text{ A}_p$$

$$P = \frac{1}{2\pi} \left[ \int_0^\pi (170 \text{ V}_p \sin \theta)(8.5 \text{ A}_p \sin \theta) d\theta \right]$$

$$P = ?$$

# Power: half sine into a resistor

$$P = \frac{1}{2\pi} \left[ \int_0^{\pi} (170 V_p \sin \theta)(8.5 A_p \sin \theta) d\theta \right]$$

$$P = (1/(2\pi)) * \int (170 * \sin(X) * 8.5 * \sin(X), X, 0, \pi)$$

$$= \frac{1}{2 \cdot \pi} \int_0^{\pi} (170 \cdot \sin(x) \cdot 8.5 \cdot \sin(x)) dx$$

$$361.25 \text{E}0$$

$$(1/(2\pi)) * \int (170 * \sin(x) * 8.5 * \sin(x), x, 0, \pi)$$

# Power for common waves

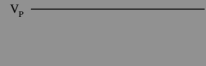
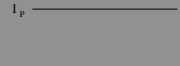
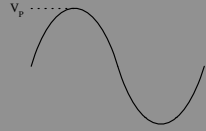
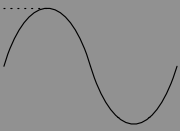
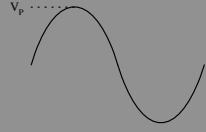
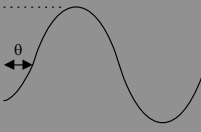
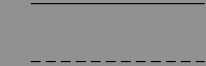
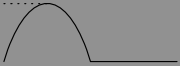
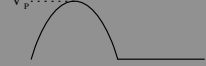
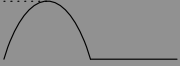
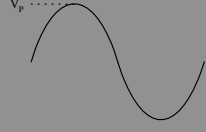
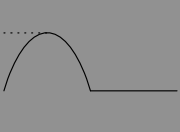


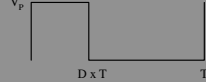

<u>v(t)</u>	<u>i(t)</u>	<u>P<sub>ave</sub></u>
		$V_p I_p$
		$\frac{V_p I_p}{2}$
		$\frac{V_p I_p}{2} \cos \theta$
		$V_{DC} \frac{I_p}{\pi}$
		$\frac{V_p I_p}{4}$
		$\frac{V_p I_p}{4}$
		$\frac{V_p I_p}{2}$
		$D V_p I_p$

Table 3-2

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# Overview

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- ◆ Average
  - definition      integrals
  - pulse    half sine                  table
  
- ◆ Root Mean Squared
  - definition      integrals
  - pulse    half sine                  table
  
- ◆ Power
  - definition
  - pulse    half sine                  table